

A Book on the fortexbook Option

The Instructors Edition

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Introduction: Instructor Solution Manual

This document contains the solutions to all problems from the historic textbook *A Book on the fortetbook Option*, by Dr. D. P. Story, *et al.*

In addition to any commented text in the source file of this document, a description of how to create a solution manual may be found in **Chapter 3**, page 35, of *A Book on the fortetbook Option*. You can learn much from reading the source file of this document as well.

You can write introductory text to the **Student Edition** and the **Instructor Edition** in the same source file by using the switch(es) `\ifisinstred` and `\ifisstudented`. If it is not compiled for the instructor edition, then it is compiled for the student edition, so normally, both of these are not needed.

The file itself was compiled using the options

```
\textbookOpts{instred,lsols}
```

found in the preamble of this document.

Chapter 1

The New eqexam

1.1 Setting the page layout

1. (a) We have, $3x + 5 = 1 \Rightarrow 3x = -4 \Rightarrow x = -\frac{4}{3}$

(b) We have

$$\begin{aligned}\frac{1}{2}(x + 5) &= \frac{1}{3}(2x - 1) \\ 3(x + 5) &= 2(2x - 1) \\ 3x + 15 &= 4x - 2 \\ x &= 17\end{aligned}$$

The solution is $x = 17$

(c) We first note that $x \neq 2$. We now solve the equation.

$$\begin{aligned}\frac{x}{x-2} + 3 &= \frac{2}{x-2} \\ x + 3(x-2) &= 2 \\ 4x - 6 &= 2 \\ x &= 2\end{aligned}$$

Since the solution, $x = 2$ is not in the domain of the equation, we conclude that the equation has **no solution**, or the solution set is $S = \emptyset$

(d) We multiply both sides by 21.

$$\begin{aligned}\frac{x+1}{3} + \frac{x+2}{7} &= 2 \\ 7(x+1) + 3(x+2) &= 42 \\ 10x + 13 &= 42 \\ 10x &= 29 \\ x &= \frac{29}{10}\end{aligned}$$

The solution is $x = 29/10$

2. (a) $(3 - 4i) - (-3 - 7i) = 3 - 4i + 3 + 7i = 6 + (7 - 4)i = 6 + 3i$

(b) $(2 + 3i)^2 = 4 + 12i + 9i^2 = 4 + 12i - 9 = \frac{-5 + 12i}{7}$

(c) We multiply the numerator and denominator by the complex conjugate of the denominator.

$$\begin{aligned}\frac{2-3i}{4+3i} &= \frac{2-3i}{4+3i} \cdot \frac{4-3i}{4-3i} \\ &= \frac{(2-3i)(4-3i)}{25} \\ &= \frac{8-6i-12i-9}{25} \\ &= \frac{-1-18i}{25}\end{aligned}$$

3. We use standard methods.

$$\begin{aligned}x^2 - 3x + 1 &= 0 \\ x^2 - 3x &= -1 \\ x^2 - 3x + \frac{9}{4} &= -1 + \frac{9}{4} \\ \left(x - \frac{3}{2}\right)^2 &= \frac{5}{4} \\ x - \frac{3}{2} &= \pm \frac{\sqrt{5}}{2} \\ x &= \frac{3}{2} \pm \frac{\sqrt{5}}{2}\end{aligned}$$

The solutions are $x = \frac{3}{2} - \frac{\sqrt{5}}{2}, \frac{3}{2} + \frac{\sqrt{5}}{2}$

4. We apply the quadratic formula:

$$\begin{aligned}x &= \frac{4 \pm \sqrt{16 - 4(1)(8)}}{2} \\ &= \frac{4 \pm \sqrt{16 - 32}}{2} \\ &= \frac{4 \pm \sqrt{-16}}{2} \\ &= \frac{4 \pm 4i}{2} \\ &= 2 \pm 2i\end{aligned}$$

The solutions are $x = 2 - 2i, 2 + 2i$.

5. We isolate the root on the LHS and square.

$$\begin{aligned}\sqrt{x-1} + 7 &= x \\ \sqrt{x-1} &= x - 7 \\ x - 1 &= (x - 7)^2 \\ x - 1 &= x^2 - 14x + 49 \\ x^2 - 15x + 50 &= 0 \\ (x - 5)(x - 10) &= 0\end{aligned}$$

The results are $x = 5, 10$, but $x = 5$ is an extraneous solution, so the solution set is $\{10\}$.

6. Let $u = x + 4$, so $u^2 - 2u - 3 = 0$. Factoring we get $(u + 1)(u - 3) = 0$ Thus $x + 4 = -1$ or $x + 4 = 3$ or $x = -5, -1$.

7. (a) A simple linear inequality:

$$\begin{aligned}\frac{1}{3}x - 2 &\geq \frac{1}{2}x + 1 \\ \Rightarrow 2x - 12 &\geq 3x + 6 \\ \Rightarrow -x &\geq 18 \\ \Rightarrow x &\leq -18\end{aligned}$$

The solution set is $S = (-\infty, -18]$

(b) A compound linear inequality,

$$\begin{aligned}-1 &\leq \frac{3 - 5x}{2} \leq 9 \\ \Rightarrow -2 &\leq 3 - 5x \leq 18 \\ \Rightarrow -5 &\leq -5x \leq 15 \\ \Rightarrow 1 &\geq x \geq -3 \quad \text{or} \quad -3 \leq x \leq 1\end{aligned}$$

The solution set is $S = [-3, 1]$

8. (a) We use standard methods,

$$\begin{aligned}|2 - x| &= |2x| \\ 2 - x = 2x \quad \text{or} \quad 2 - x &= -2x \\ 3x = 2 \quad \text{or} \quad x &= -2 \\ x = 2/3 \quad \text{or} \quad x &= -2\end{aligned}$$

The solutions are $x = 2/3, -2$

(b) We use standard techniques,

$$\begin{aligned}|x - 4| &\leq 6 \\ -6 &\leq x - 4 \leq 6 \\ -2 &\leq x \leq 10\end{aligned}$$

The solution is $S = [-2, 10]$

(c) We use standard methods again.

$$\begin{aligned}|2x + 1| &> 4 \\ 2x + 1 > 4 \quad \text{or} \quad 2x + 1 &< -4 \\ 2x > 3 \quad \text{or} \quad 2x &< -5 \\ x > 3/2 \quad \text{or} \quad x &< -5/2\end{aligned}$$

Solution: $S = (-\infty, -5/2) \cup (3/2, +\infty)$

9. We first find how much was invested in each account. Let x = amt invested at 6%, so $4900 - x$ was invested at 8%. The problem states that

$$.06x = .08(4900 - x) \Rightarrow .06x = 392 - .08x \Rightarrow 0.14x = 392 \Rightarrow x = 2800.$$

So, Mr. Gilg invested \$2800 at 6% and earned \$168 ($\$168 = .06 \cdot \2800). The interest earned for the other account was the same as the first, so he earned \$168 there too. The total interest earned then by the famous Mr. Gilg is $I = \$168 + \$168 = \$336$

10. Note that the coefficients of y are equal but opposite in sign. So we will use the *elimination method* and add the two equations together to get $5x = -5$, so $x = -1$. Substituting this into the first equation, we get $y = 2 - 2(-1) = 4$. The point of intersection of these two lines is $(-1, 4)$.

1.2 Another Section

1. (a) We use the distance formula:

$$d(P, Q) = \sqrt{(2+4)^2 + (-3-2)^2} = \sqrt{61}$$

(b) We use the midpoint formula:

$$M = \left(\frac{-4+2}{2}, \frac{2+(-3)}{2} \right) = \left(-1, -\frac{1}{2} \right)$$

2. For the x -intercepts, we set $y = 0$: $x^2 - 6x + 8 = 0 \Rightarrow (x-2)(x-4) = 0 \Rightarrow x = 2, 4$

3. We complete the square:

$$\begin{aligned} x^2 + y^2 - 4x + 12y = -1 &\Rightarrow (x^2 - 4x + 4) + (y^2 + 12y + 36) = -1 + 4 + 36 \\ &\Rightarrow \boxed{(x-2)^2 + (y+6)^2 = 39} \end{aligned}$$

4. (a) We calculate the slope of a line.

$$m = \frac{-2-4}{-4-(-9)} = -\frac{6}{5}$$

(b) Use the point-slope form: $y - 2 = \frac{1}{3}(x + 3) \Rightarrow y = \frac{1}{3}x + 3$

(c) The given line has slope $m = -\frac{1}{2}$ and the target line must pass through $(-3, 0)$, so our equation is $y - 0 = -\frac{1}{2}(x + 3) \Rightarrow y = -\frac{1}{2}x - \frac{3}{2}$

5. (a) We have, $f(2) = \frac{2}{2^2 + 1} = \frac{2}{5}$

(b) We have, $f(-3) = \frac{-3}{(-3)^2 + 1} = \frac{-3}{9 + 1} = -\frac{3}{10}$

(c) We have, $f(2x) = \frac{2x}{(2x)^2 + 1} = \frac{2x}{2x^2 + 1}$

(d) We perform the usual tests.

$$f(-x) = \frac{-x}{(-x)^2 + 1} = -\frac{x}{x^2 + 1} = -f(x)$$

The function is odd.

6. (a) Because of the square root function, we require $3 - x \geq 0$, or $x \leq 3$. In interval notation, the domain is $(-\infty, 3]$

(b) The denominator is factored into $(x+1)(x-1)$; as a result, the domain consists of all numbers x except where the denominator is zero. From the factorization, we see that the domain is $\{x \mid x \neq -1, x \neq 1\}$, or in interval notation, we have $(-\infty, -1) \cup (-1, 1) \cup (1, +\infty)$

Chapter 2

The fortextbook option

2.1 Building a sound foundation

1. (a) We have

$$(fg)(-2) = f(-2)g(-2) = (-5)(3) = -15$$

(b) We have

$$\left(\frac{g}{f}\right)(x) = \frac{g(x)}{f(x)} = \frac{2x^2 - 5}{4x + 3}$$

(c) Composing, $(f \circ f)(x) = f(f(x)) = f(4x + 3) = 4(4x + 3) + 3 = 16x + 15$

(d) Composing, $(f \circ g)(x) = f(g(x)) = f(2x^2 - 5) = 4(2x^2 - 5) + 3 = 8x^2 - 17$

2. It is clear that if $f(x) = \sqrt[4]{x}$ and $g(x) = 3x^2 + 1$, then $H(x) = (f \circ g)(x)$. Another choice is $f(x) = \sqrt[4]{3x + 1}$ and $g(x) = x^2$.

3. Let f be an invertible function. Suppose $f(-2) = 17$. Find $f^{-1}(17) = \boxed{-2}$; consequently, we have $(f^{-1} \circ f)(-2) = \boxed{-2}$.

4. (a) Removing the functional notation, we have, $y = 1 - \frac{1}{x}$. Interchange the roles of x and y , and solve for y . We have...

$$x = 1 - \frac{1}{y} \quad \text{interchange } x \text{ and } y$$

$$\frac{1}{y} = 1 - x \quad \text{add } 1/y \text{ and subtract } x, \text{ both sides}$$

$$y = \frac{1}{1 - x} \quad \text{take reciprocal both sides}$$

$$g^{-1}(x) = \frac{1}{1 - x} \quad x \neq 1, \text{ use functional notation}$$

(b) $\text{Rng}(g) = (-\infty, 1) \cup (1, \infty)$

5. $f(x) = a(x - h)^2 + k$ is the standard form. With the vertex information, we have $f(x) = a(x - 2)^2$, we need only find the value of a . For that we use the point P : $3 = a(4 - 2)^2 \Rightarrow 4a = 3 \Rightarrow a = 3/4$. The final form for the function is $f(x) = \frac{3}{4}(x - 2)^2$

6. We use the vertex formula, $h = -b/(2a) = -(-8)/4 = 2$, and so $h = f(2) = 8 - 16 + 5 = -3$.

7. We use the vertex formula, $h = -b/(2a) = -(-1)/2 = 1/2$. A **minimum** occurs since the leading coefficient is positive, which means the parabola opens up, the vertex is a minimum.

8. For a polynomial of degree 12, according to theory, the maximum number of zeros is 12, and the maximum number of turning points is 11.
9. List the *horizontal asymptotes* (H.A.) and the *vertical asymptotes* (V.A.) of the rational function below, and label each vertical asymptote as *even* or *odd*.

$$f(x) = \frac{2x^4 - 3x^2}{(x+3)^2(x^2-4)}$$

H.A.: $y = 2$ V.A.: $x = -3$ (even), $x = -2$ (odd), $x = 2$ (odd)

10. (a) We have $y = \frac{k}{x}$, but $8 = \frac{k}{2} \Rightarrow k = 16$. thus, $y = \frac{16}{x}$.

(b) We have $z = kx^2\sqrt{y}$, but $9 = k2^2\sqrt{4} \Rightarrow 9 = 8k \Rightarrow k = 9/8$; thus $y = \frac{9}{8}x^2\sqrt{y}$.

2.2 Another awesome section

1. (a) $f(x) = 3^{1-x}$, $f(3.2) = 0.089$

(b) $f(x) = e^{x/2}$, $f(4.2) = 8.166$

(c) $f(x) = -\left(\frac{1}{2}\right)^{x+1}$, $f(-3.5) = -5.657$

2. We have $2^{-x+1} = 2^4 \Rightarrow -x+1 = 4 \Rightarrow x = -3$

3. Convert $81^{1/2} = 9$ into a logarithmic form. It is apparent that, $\log_{81}(9) = 1/2$

4. (a) $\log_4(x) = -2 \Rightarrow x = 4^{-2} = \boxed{1/16}$

(b) $\log_{16}(\sqrt{x-1}) = \frac{1}{4} \Rightarrow \sqrt{x-1} = 16^{1/4} \Rightarrow \sqrt{x-1} = 2 \Rightarrow x-1 = 4 \Rightarrow \boxed{x = 5}$

5. We require $x-4 > 0$ or that $x > 4$.

6. (a) We use one of the basic log properties: $a^{\log_a(x)} = x$. So here $4^{\log_4(1.4)} = 1.4$.

(b) We use the basic identity again, $a^{\log_a(x)} = x$: $e^{\ln(2x+1)} = 11 \Rightarrow 2x+1 = 11 \Rightarrow x = 5$

7. (a) $\log_4(16x^8) = \boxed{2 + 8\log_4(x)}$

We use the properties of logarithms:

$$\log_4(16x^8) = \log_4(16) + 8\log_4(x) = \log_4(4^2) + 8\log_4(x) = \boxed{2 + 8\log_4(x)}$$

(b) We have,

$$\log\left(\sqrt{\frac{x}{4}}\right) = \log\left(\frac{x}{4}\right)^{1/2} = \frac{1}{2}\log\left(\frac{x}{4}\right) = \boxed{\frac{1}{2}(\log(x) - \log(4))}$$

(c) We use the properties of logarithms:

$$\begin{aligned} \log\frac{x(x-1)^4}{(x+1)^3} &= \log(x(x-1)^4) - \log(x+1)^3 = \log(x) + \log(x-1)^4 - 3\log(x+1) \\ &= \boxed{\log(x) + 4\log(x-1) - 3\log(x+1)} \end{aligned}$$

8. (a) $\log_7(12) - \log_7(x) = \log_7\left(\frac{12}{x}\right)$

(b) $\frac{1}{2}(\log(x) + 3\log(y)) = \frac{1}{2}(\log(x) + \log(y^3)) = \frac{1}{2}\log(xy^3) = \log(xy^3)^{1/2}$

9. (a) $\log(310.4) \approx \boxed{2.4919}$
 (b) $\ln(310.4) \approx \boxed{5.7379}$
 (c) $\log_3(11.4) \approx \boxed{2.2172}$
 (d) $\log_{1/2}(11.4) \approx \boxed{-3.5110}$

10. (a) We use standard techniques, take logs of both sides, and solve for x .

$$5^{2x} = 7.3 \Rightarrow \ln 5^{2x} = \ln 7.3 \Rightarrow 2x \ln 5 = \ln 7.3 \Rightarrow x = \frac{\ln 7.3}{2 \ln 5} \approx 0.6176$$

(b) We use standard techniques, take logs of both sides, and solve for x .

$$2^x = 3^{x+1} \Rightarrow \ln 2^x = \ln 3^{x+1} \Rightarrow x \ln 2 = (x+1) \ln 3 \Rightarrow x \ln 2 = x \ln 3 + \ln 3$$

$$\Rightarrow x(\ln 2 - \ln 3) = \ln 3 \Rightarrow x = \frac{\ln(3)}{\ln(2) - \ln(3)} \approx -2.7095$$

11. (a) $\log_5(2x - 1) = 1.1 \Rightarrow 2x - 1 = 5^{1.1} \Rightarrow x = \frac{1 + 5^{1.1}}{2} \approx 3.4365$

(b) We have,

$$\log_2(x - 1) - \log_2(x - 2) = 3 \Rightarrow \log_2 \frac{x - 1}{x - 2} = 3 \Rightarrow \frac{x - 1}{x - 2} = 2^3$$

$$\Rightarrow x - 1 = 8(x - 2) \Rightarrow x - 1 = 8x - 16 \Rightarrow 15 = 7x \Rightarrow x = \frac{15}{7} \approx 2.1429$$

2.3 One more time!

- Recall the point $(\cos(x), \sin(x))$ lies on the unit circle, hence, the point satisfies the equation $\sin^2(x) + \cos^2(x) = 1$.
- If we divide both sides of $\sin^2(x) + \cos^2(x) = 1$ by $\cos^2(x)$, we obtain the identity $\tan^2(x) + 1 = \sec^2(x)$.
- If we divide both sides of $\sin^2(x) + \cos^2(x) = 1$ by $\sin^2(x)$, we obtain the identity $1 + \cot^2(x) = \csc^2(x)$.
- Take the addition formula for the sine function,

$$\sin(x + y) = \sin(x) \cos(y) + \cos(x) \sin(y)$$

and put $x = y$ to obtain the required equation: $\sin(2x) = 2 \sin(x) \cos(x)$.

- Take the addition formula for the cosine function,

$$\cos(x + y) = \cos(x) \cos(y) - \sin(x) \sin(y)$$

and put $x = y$ to obtain the basic equation, $\cos(2x) = \cos^2(x) - \sin^2(x)$. Now substitute $\sin^2(x) = 1 - \cos^2(x)$ into this equation to obtain $\cos(2x) = 2 \cos^2(x) - 1$; substitute $\cos^2(x) = 1 - \sin^2(x)$ into the first equation, we obtain the last variation, $\cos(2x) = 1 - 2 \sin^2(x)$

- The addition formula for tangent is

$$\tan(x + y) = \frac{\tan(x) + \tan(y)}{1 - \tan(x) \tan(y)}$$

Now, setting $y = x$, we obtain, $\tan(2x) = \frac{2 \tan(x)}{1 - \tan^2(x)}$

- $\sinh(x) = (e^x - e^{-x})/2$
- $\cosh(x) = (e^x + e^{-x})/2$

2.4 Once more, once!

1. (a) The function $f(x) = (4.3)^x$ is an exponential function with a base of $a = \underline{4.3}$.
- (b) T (T or F) One of the properties of logarithms is $\log_a(x) - \log_a(y) = \log_a(x/y)$
- (c) The correct alternative is , the domain of $f(x) = \log_a(x)$ is $\text{Dom}(f) = \underline{\quad}$.
- (d) The inverse of the function $f(x) = 7^x$ is $f^{-1}(x) = \underline{\log_7(x)}$.

Demo Problem Set

1. Solve the equation
- $2x + 5 = -2$
- for
- x
- . Indeed,

$$\begin{aligned} 2x + 5 &= -2 && \text{given} \\ 2x &= -7 && \text{subtract 5 both sides} \\ x &= \boxed{-\frac{7}{2}} && \text{divide by 2 both sides} \end{aligned}$$

2.6 Review Exercises

Section 2.2

1. (a) We have

$$\begin{aligned} \frac{1}{2}(x + 5) &= \frac{1}{3}(2x - 1) \\ 3(x + 5) &= 2(2x - 1) \\ 3x + 15 &= 4x - 2 \\ x &= 17 \end{aligned}$$

The solution is $\boxed{x = 17}$

- (b) We have,

$$6x + 5 = 3x + 1 \Rightarrow 3x = -4 \Rightarrow \boxed{x = -\frac{4}{3}}$$

2. We use standard methods.

$$\begin{aligned} x^2 - 3x + 1 &= 0 && (x - \frac{3}{2})^2 = \frac{5}{4} \\ x^2 - 3x &= -1 && x - \frac{3}{2} = \pm \frac{\sqrt{5}}{2} \\ x^2 - 3x + \frac{9}{4} &= -1 + \frac{9}{4} && x = \frac{3}{2} \pm \frac{\sqrt{5}}{2} \end{aligned}$$

The solutions are $\boxed{x = \frac{3}{2} - \frac{\sqrt{5}}{2}, \frac{3}{2} + \frac{\sqrt{5}}{2}}$

3. (a) A simple linear inequality:

$$\begin{aligned} \frac{1}{3}x - 2 &\geq \frac{1}{2}x + 1 \\ \Rightarrow 2x - 12 &\geq 3x + 6 \\ \Rightarrow -x &\geq 18 \\ \Rightarrow x &\leq -18 \end{aligned}$$

The solution set is $S = (-\infty, -18]$

(b) We use standard techniques,

$$\begin{aligned} |x - 4| &\leq 6 \\ -6 &\leq x - 4 \leq 6 \\ -2 &\leq x \leq 10 \end{aligned}$$

The solution is $S = [-2, 10]$

4. The given line has slope $m = -\frac{1}{2}$ and the target line must pass through $(-3, 0)$, so our equation is $y - 0 = -\frac{1}{2}(x + 3) \Rightarrow y = -\frac{1}{2}x - \frac{3}{2}$

Section 2.3

5. (a) We use standard methods.

$$\begin{aligned} f(x) &= 3 - 5x \Rightarrow y = 3 - 5x \\ \Rightarrow x &= 3 - 5y \Rightarrow 5y = 3 - x \\ \Rightarrow y &= \frac{3 - x}{5} \Rightarrow f^{-1}(x) = \frac{3 - x}{5} \end{aligned}$$

(b) We use standard methods.

$$\begin{aligned} f(x) &= 6x^3 + 2 \Rightarrow y = 6x^3 + 2 \\ \Rightarrow x &= 6y^3 + 2 \Rightarrow 6y^3 = x - 2 \\ \Rightarrow y &= \sqrt[3]{\frac{x - 2}{6}} \Rightarrow f^{-1}(x) = \sqrt[3]{\frac{x - 2}{6}} \end{aligned}$$

6. (a) We have...

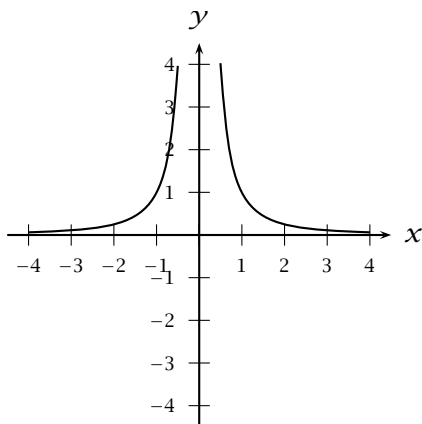
$$\begin{aligned} 9^{2x} &= 27 \Rightarrow 3^{4x} = 3^3 \\ \Rightarrow 4x &= 3 \Rightarrow x = 3/4 \end{aligned}$$

(b) We have...

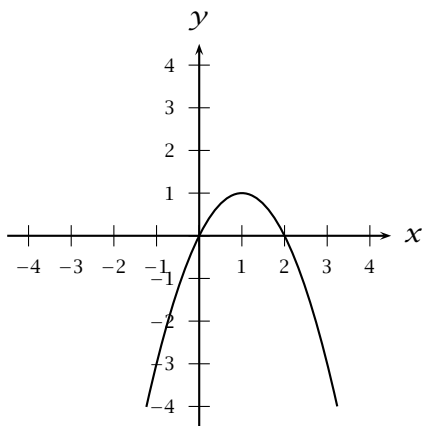
$$\begin{aligned} x + 1 &= -4x \Rightarrow 5x = -1 \\ \Rightarrow x &= -1/5 \end{aligned}$$

Chapter 2. Chapter Quiz

1. (a) Graph
- $f(x) = \frac{1}{x^2}$
- .



1. (b) Graph
- $f(x) = 1 - (x - 1)^2$
- .



2. (a) We have

$$\left(\frac{g}{f}\right)(x) = \frac{g(x)}{f(x)} = \frac{2x^2 - 5}{4x + 3}$$

- (b) Composing,

$$\begin{aligned} (f \circ g)(x) &= f(g(x)) = f(2x^2 - 5) \\ &= 4(2x^2 - 5) + 3 \\ &= \boxed{8x^2 - 17} \end{aligned}$$

3. For a polynomial of degree 17, according to theory, the maximum number of zeros is
- 17
- , and the maximum number of turning points is
- 16
- .

4. Removing the functional notation, we have, $y = 3x + 2$. Interchange the roles of x and y , and solve for y . We have...

$$\begin{aligned} x &= 3y + 2 && \text{interchange } x \text{ and } y \\ 3y &= x - 2 && \text{subtract 2, both sides} \\ y &= \frac{x - 2}{3} && \text{divide by 3} \\ g^{-1}(x) &= \frac{x - 2}{3} && \text{use functional notation} \end{aligned}$$

The domain is $(-\infty, \infty)$.

5. We use the vertex formula, $h = -b/(2a) = -(-8)/4 = 2$, and so $h = f(2) = 8 - 16 + 5 = -3$. The coordinates of the vertex is then $V(2, -3)$. Because the coefficient of x^2 is positive, the parabola opens up, which implies the vertex is a *minimum*.
6. We have $y = \frac{k}{x}$, but $8 = \frac{k}{4} \Rightarrow k = 32$. thus, $y = \frac{32}{x}$.
7. (a) We use the properties of logarithms:

$$\begin{aligned} \log \frac{x(x-1)^4}{(x+1)^3} &= \log(x(x-1)^4) - \log(x+1)^3 = \log(x) + \log(x-1)^4 - 3\log(x+1) \\ &= \boxed{\log(x) + 4\log(x-1) - 3\log(x+1)} \end{aligned}$$

(b) We use the properties of logarithms.

$$\frac{1}{2}(\log(x) + 3\log(y)) = \frac{1}{2}(\log(x) + \log(y^3)) = \frac{1}{2}\log(xy^3) = \log(xy^3)^{1/2}$$

8. (a) We use standard techniques, take logs of both sides, and solve for x .

$$5^{2x} = 7.3 \Rightarrow \ln 5^{2x} = \ln 7.3 \Rightarrow 2x \ln 5 = \ln 7.3 \Rightarrow \boxed{x = \frac{\ln 7.3}{2 \ln 5} \approx 0.6176}$$

(b) We solve by converting log to exponential.

$$\log_5(2x - 1) = 1.1 \Rightarrow 2x - 1 = 5^{1.1} \Rightarrow \boxed{x = \frac{1 + 5^{1.1}}{2} \approx 3.4365}$$